CAMBRIDGE INTERNATIONAL EXAMINATIONS

Cambridge International General Certificate of Secondary Education

MARK SCHEME for the October/November 2015 series

0606 ADDITIONAL MATHEMATICS

0606/13 Paper 1, maximum raw mark 80

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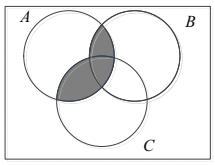
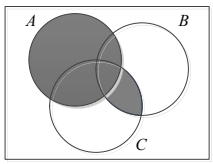
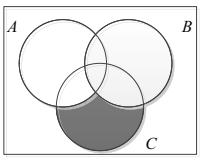
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Abbreviations

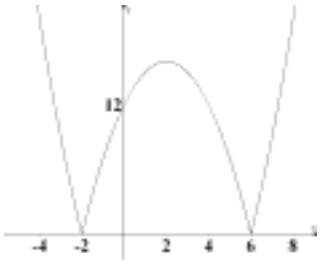
Awrt answers which round to
Cao correct answer only
dep dependent
FT follow through after error
isw ignore subsequent working
oe or equivalent
rot rounded or truncated
SC Special Case
soi seen or implied
www without wrong working

1 **(i)**		B1	
(ii)		B1	
(iii)		B1	
2	$\cos\left(3x-\frac{\pi}{4}\right)=(\pm)\frac{1}{\sqrt{2}}$ oe	M1	division by 2 and square root
	$3x-\frac{\pi}{4}=-\frac{\pi}{4},\ \frac{\pi}{4},\ \frac{3\pi}{4}$		
	$x=\left(-\frac{\pi}{4}+\frac{\pi}{4}\right)\div 3,\ \left(\frac{\pi}{4}+\frac{\pi}{4}\right)\div 3,\ \left(\frac{3\pi}{4}+\frac{\pi}{4}\right)\div 3$ oe	DM1	correct order of operations in order to obtain a solution
	$x=0$ and $\frac{\pi}{6}$ (or 0 and 0.524)	A2/1/0	A2 for 3 solutions and no extras in the range A1 for 2 solutions A0 for one solution or no solutions
	$x=\frac{\pi}{3}$ (or 1.05)		

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3	(a)	$\begin{pmatrix} 12 & 16 & 4 \\ 30 & 32 & 10 \end{pmatrix}$	B2,1,0	B2 for 6 elements correct, B1for 5 elements correct
	(b)	$\begin{pmatrix} 28 & -24 \\ -8 & 76 \end{pmatrix} = m\begin{pmatrix} 4 & 6 \\ 2 & -8 \end{pmatrix} + n\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$	B2,1,0	B2 for 4 correct elements in $\mathbf{X}^2$ B1 for 3 correct elements in $\mathbf{X}^2$
		$-24 = 6m$ or $-8 = 2m$ giving $m = -4$	B1	For $m = -4$ using correct **I**
		$28 = 4m + n$ or $76 = -8m + n$ $n = 44$	M1 A1	complete method to obtain n
	(c)	$a^2 - 6 = 0$ so $a = \pm\sqrt{6}$	B2,1,0	B2 for $a = \pm\sqrt{6}$ or $a = \pm 2.45$, with no incorrect statements seen or B1 for $a = \pm\sqrt{6}$ or $a = \pm 2.45$ seen or B1 for $a = \sqrt{6}$ and no incorrect working
4	(i)	$\frac{1}{2}\left(4\sqrt{3}+1\right) \times BC = \frac{47}{2}$	B1	correct use of the area
		$BC = \frac{47}{\left(4\sqrt{3}+1\right)} \times \frac{\left(4\sqrt{3}-1\right)}{\left(4\sqrt{3}-1\right)}$	M1	correct rationalisation
		$BC = 4\sqrt{3} - 1$	A1	Dependent on all method being seen
		Alternative method		
		$\frac{1}{2}\left(4\sqrt{3}+1\right) \times BC = \frac{47}{2}$ $\left(4\sqrt{3}+1\right)\left(a\sqrt{3}+b\right) = 47$	B1	
		Leading to $12a + b = 47$ and $a + 4b = 0$ Solution of simultaneous equations	M1	
		$BC = 4\sqrt{3-1}$	A1	Dependent on all method seen including solution of simultaneous equations
	(ii)	$\left(4\sqrt{3}+1\right)^2 + \left(4\sqrt{3}-1\right)^2$		
		$= \left(48 + 8\sqrt{3} + 1\right) + \left(48 - 8\sqrt{3} + 1\right)$	B1FT	6 correct FT terms seen
		$AC^2 = 98$ $AC = 7\sqrt{2}$ **or** $p = 7$	B1cao	98 and $7\sqrt{2}$ or 98 and $p = 7$

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5	When $x = \frac{\pi}{4}$, $y = 2$	B1	$y = 2$
	$\frac{dy}{dx} = 5\sec^2 x$	B1	$5\sec^2 x$
	When $x = \frac{\pi}{4}$, $\frac{dy}{dx} = 10$	B1	10 from differentiation
	Equation of normal $y - 2 = -\frac{1}{10}\left(x - \frac{\pi}{4}\right)$	M1	$y - their 2 = -\frac{1}{their 10}\left(x - \frac{\pi}{4}\right)$
	$10y + x - 20 - \frac{\pi}{4} = 0$ or $10y + x - 20.8 = 0$ oe	A1	allow unsimplified
6 (i)		B1 B1 B1	shape intercepts on x-axis intercept on y-axis for a curve with a maximum and two arms
(ii)		M1	$(2, \pm 16)$ seen or $(2, k)$ where $k > 0$
	$(2, 16)$	A1	(2, 16) or $x = 2$ **and** $y = 16$ only
(iii)	$k = 0$	B1	
	$k > 16$	B1	

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7		$\frac{dy}{dx} = 2\sin 3x \quad (+c)$	B1	$2\sin 3x$
		$4\sqrt{3} = 2\frac{\sqrt{3}}{2} + c$	M1	finding constant using $\frac{dy}{dx} = k\sin 3x + c$ making use of $\frac{dy}{dx} = 4\sqrt{3}$ and $x = \frac{\pi}{9}$
		$\frac{dy}{dx} = 2\sin 3x + 3\sqrt{3}$	A1	Allow with $c = 5.20$ or $\sqrt{27}$
		$y = -\frac{2}{3}\cos 3x + 3\sqrt{3}x \quad (+d)$	B1FT	FT integration of *their* $k\sin 3x$
		$-\frac{1}{3} = -\frac{2}{3}\cos\frac{\pi}{3} + 3\sqrt{3}\left(\frac{\pi}{9}\right) + d$	M1	finding constant d for $k\cos 3x + cx + d$
		$y = -\frac{2}{3}\cos 3x + 3\sqrt{3}x - \frac{\sqrt{3}}{3}\pi$	A1	Allow $y = -0.667\cos 3x + 5.20x - 0.577\pi$ or better
8	**(a)**	$(2+kx)^8 = 256 + 1024kx + 1792k^2x^2 + 1792k^3x^3$		
		$k = \frac{1}{4}$	B1	
		$p = 112$	B1FT	FT 1792 multiplied by *their* k^2
		$q = 28$	B1FT	FT 1792 multiplied by *their* k^3
	(b)	${}^9C_3x^6\left(-\frac{2}{x^2}\right)^3$	M1	correct term seen
		$84x^6\left(-\frac{8}{x^6}\right)$ leading to -672	DM1 A1	Term selected and 2^3 and ${}^9C_3$ correctly evaluated

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9	(a) (i)	Number of arrangements with Maths books as one item = 4! or $4 \times 3!$	M1	$4!(\times 2)$ or $4 \times 3!(\times 2)$ oe
		or Maths books can be arranged 2! ways and History 3! ways = $2! \times 3!$		$2! \times 3!(\times 4)$ or $2 \times 3!(\times 4)$ oe
		$2 \times 4!$ or $2 \times 4 \times 3!$ or $4 \times 2 \times 3! = 48$	A1	A1 for 48
	(ii)	$5! - 48$ or $6 \times 2 \times 3!$	M1	$5!$ – *their* answer to (i) or for $6 \times 2 \times 3$
		72	A1	
	(b) (i)	3003	B1	
	(ii)	$3003 - 6 - 135$	M1	*their* answer to (i) $- 6 -^{6} C_{4} \times 9$
			B1	135 subtracted
		2862	A1	
		or		
		2M 3W = 720	M1	complete correct method using 4 cases, may be implied by working. Must have at least one correct
		3M 2W = 1260		
		4M 1W = 756		
		5M = 126	B1	any 3 correct
		2862	A1	

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10 (i)	$10^2 = 6^2 + 6^2 - 2 \times 6 \times 6 \times \cos ABC$ or $\sin\left(\frac{ABC}{2}\right) = \frac{5}{6}$ or $ABC = \pi - \sin^{-1}\frac{10\sqrt{11}}{36}$	M1	correct cosine rule statement or correct statement for $\sin\frac{ABC}{2}$ or equating areas oe
	$ABC = 1.9702$	A1	1.9702 or better
(ii)	$XY = 2$	B1	for XY (may be implied by later work, allow on diagram)
	Arc length $6\left(\frac{\pi - 1.970}{2}\right)$ oe	B1	correct arc length (unsimplified)
	Perimeter = $2 + 2\left(6\left(\frac{\pi - 1.970}{2}\right)\right)$ $= 9.03$	M1 A1	*their* 2 + 2 × 6 × *their* angle *C*
(iii)	$\left(\frac{1}{2} \times 6^2\left(\frac{\pi - 1.970}{2}\right) - \frac{1}{2} \times 5 \times \sqrt{11}\right) \times 2$	M1 M1	sector area using *their C* area of Δ *ABM* where *M* is the midpoint of *AC*, or (Δs *ABY* and *BXY*) or Δ*ABC*
	= 4.50 or 4.51 or better	A1	Answers to 3sf or better

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11	$x^2 - 2x - 3 = 0$ or $y^2 - 6y + 5 = 0$	M1	substitution and simplification to obtain a three term quadratic equation in one variable
	leading to (3, 5) and (–1, 1)	A1,A1	A1 for each 'pair' from a correct quadratic equation, correctly obtained.
	Midpoint (1, 3)	B1cao	midpoint
	(Gradient – 1) Perpendicular bisector $y = 4 - x$	M1	perpendicular bisector, must be using *their* perpendicular gradient and *their* midpoint
	Meets the curve again if $x^2 + 10x - 15 = 0$ or $y^2 - 18y + 41 = 0$	M1	substitution and simplification to obtain a three term quadratic equation in one variable.
	leading to $x = -5 \pm 2\sqrt{10}$, $y = 9 \mp 2\sqrt{10}$	A1,A1	A1 for each 'pair'
	$CD^2 = \left(4\sqrt{10}\right)^2 + \left(4\sqrt{10}\right)^2$	M1	Pythagoras using *their* coordinates from solution of second quadratic. $(x_1 - x_2)^2 + (y_1 - y_2)^2$ must be seen if not using correct coordinates.
	$CD = 8\sqrt{5}$	A1	A1 for $8\sqrt{5}$ from $\sqrt{320}$ and all correct so far.

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12	**(a)**	$2^{2x-1} \times 2^{2(x+y)} = 2^7$ and $\frac{3^{2(2y-x)}}{3^{3(y-4)}} = 1$	M1	expressing 4^{x+y}, 128 as powers of 2 and 9^{2y-x}, 27^{y-4} as powers of 3
		$2x - 1 + 2(x + y) = 7$ oe	A1	Correct equation from correct working
		$2(2y - x) = 3(y - 4)$ oe	A1	Correct equation from correct working
		leading to $x = 4,\ y = -4$	A1	for both
		<u>Example of Alternative method</u>		
		Method mark as above	M1	As before
		$2x - 1 + 2(x + y) = 7$	A1	One of the correct equations in x and y
		leading to $y = \frac{(8 - 4x)}{2}$		
		Correctly substituted in $\frac{3^{2(2y-x)}}{3^{3(y-4)}} = 1$		
		Leading to $2\left(\frac{2(8-4x)}{2} - x\right) = 3\left(\frac{(8-4x)}{2} - 4\right)$	A1	Correct, unsimplified, equation in x or y only
		Leading to $x = 4$ and $y = -4$	A1	Both answers
	(b)	$(2(5^z) - 1)(5^z + 1) = 0$	M1	solution of quadratic
		leading to $2.5^z = 1$ $\quad (5^z = -1)$	A1	correct solution
		$5^z = 0.5$	DM1	correct attempt to solve $2.5^z = k$, where k is positive
		$z = \frac{\log 0.5}{\log 5}$ or $z = -0.431$ or better	A1	must have one solution only

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