Cambridge International A Level

**Cambridge Assessment International Education**
Cambridge International Advanced Level

**MATHEMATICS** **9709/73**

Paper 7 **October/November 2019**

MARK SCHEME

Maximum Mark: 50

**Published**

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

Cambridge International will not enter into discussions about these mark schemes.

Cambridge International is publishing the mark schemes for the October/November 2019 series for most Cambridge IGCSE™, Cambridge International A and AS Level components and some Cambridge O Level components.



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## Generic Marking Principles

These general marking principles must be applied by all examiners when marking candidate answers. They should be applied alongside the specific content of the mark scheme or generic level descriptors for a question. Each question paper and mark scheme will also comply with these marking principles.

GENERIC MARKING PRINCIPLE 1:
Marks must be awarded in line with:

- the specific content of the mark scheme or the generic level descriptors for the question
- the specific skills defined in the mark scheme or in the generic level descriptors for the question
- the standard of response required by a candidate as exemplified by the standardisation scripts.

GENERIC MARKING PRINCIPLE 2:
Marks awarded are always **whole marks** (not half marks, or other fractions).

GENERIC MARKING PRINCIPLE 3:
Marks must be awarded **positively**:

- marks are awarded for correct/valid answers, as defined in the mark scheme. However, credit is given for valid answers which go beyond the scope of the syllabus and mark scheme, referring to your Team Leader as appropriate
- marks are awarded when candidates clearly demonstrate what they know and can do
- marks are not deducted for errors
- marks are not deducted for omissions
- answers should only be judged on the quality of spelling, punctuation and grammar when these features are specifically assessed by the question as indicated by the mark scheme. The meaning, however, should be unambiguous.

GENERIC MARKING PRINCIPLE 4:
Rules must be applied consistently e.g. in situations where candidates have not followed instructions or in the application of generic level descriptors.

GENERIC MARKING PRINCIPLE 5:
Marks should be awarded using the full range of marks defined in the mark scheme for the question (however; the use of the full mark range may be limited according to the quality of the candidate responses seen).

GENERIC MARKING PRINCIPLE 6:
Marks awarded are based solely on the requirements as defined in the mark scheme. Marks should not be awarded with grade thresholds or grade descriptors in mind.

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## Mark Scheme Notes

The following notes are intended to aid interpretation of mark schemes in general, but individual mark schemes may include marks awarded for specific reasons outside the scope of these notes.

### Types of mark

**M** Method mark, awarded for a valid method applied to the problem. Method marks are not lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. Correct application of a formula without the formula being quoted obviously earns the M mark and in some cases an M mark can be implied from a correct answer.

**A** Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated method mark is earned (or implied).

**B** Mark for a correct result or statement independent of method marks.

**DM** or **DB** When a part of a question has two or more "method" steps, the M marks are generally independent unless the scheme specifically says otherwise; and similarly, when there are several B marks allocated. The notation DM or DB is used to indicate that a particular M or B mark is dependent on an earlier M or B (asterisked) mark in the scheme. When two or more steps are run together by the candidate, the earlier marks are implied and full credit is given.

**FT** Implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A or B marks are given for correct work only.

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**Abbreviations**

| | |
|---|---|
| AEF/OE | Any Equivalent Form (of answer is equally acceptable) / Or Equivalent |
| AG | Answer Given on the question paper (so extra checking is needed to ensure that the detailed working leading to the result is valid) |
| CAO | Correct Answer Only (emphasising that no “follow through” from a previous error is allowed) |
| CWO | Correct Working Only |
| ISW | Ignore Subsequent Working |
| SOI | Seen Or Implied |
| SC | Special Case (detailing the mark to be given for a specific wrong solution, or a case where some standard marking practice is to be varied in the light of a particular circumstance) |
| WWW | Without Wrong Working |
| AWRT | Answer Which Rounds To |

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| Question | Answer | Marks | Guidance |
|---|---|---|---|
| 1(i) | 9.6, 12.4 | **B1 B1** | |
| | | **2** | |
| 1(ii) | 6.6, 49.6 | **B1 B1** | |
| | | **2** | |

| Question | Answer | Marks | Guidance |
|---|---|---|---|
| 2(i) | $\left(\lambda\left(=2\times2.4\right)=4.8\right)$<br>$e^{-4.8}\left(1+4+\frac{4.8^2}{2}+\frac{4.8^3}{3!}\right)$ | **M1** | Any $\lambda$ |
| | 0.294 (3 sf) | **A1** | |
| | | **2** | |
| 2(ii) | $\left(\lambda\left(=60\times2.4\right)=144\right)$<br>N('144', '144') | **M1** | N and $\sigma^2=\mu$ SOI |
| | $\frac{139.5-'144'}{\sqrt{'144'}}\left(=-0.375\right)$ | **M1** | Allow with no continuity correction |
| | $\phi$('0.375') | **M1** | Correct area consistent with their working |
| | 0.646 (3 sf) | **A1** | |
| | | **4** | |

| Question | Answer | Marks | Guidance |
|---|---|---|---|
| 3(i) | Assume population is normally distributed | **B1** | |
| | $\bar{x} = 25.9$ | **B1** | Allow $\frac{259}{10}$ |
| | $z = 2.17$ | **B1** | |
| | $'25.9' \pm z \times \frac{3}{\sqrt{10}}$ | **M1** | Must have correct form and $z$. |
| | 23.8 to 28.0 (3 sf) | **A1** | CWO |
| | | **5** | |
| 3(ii) | $0.03^2$ (=0.0009) | **B1** | |
| | | **1** | |

| Question | Answer | Marks | Guidance |
|---|---|---|---|
| 4 | Assume trains are independent OR probability of being on time is constant | **B1** | Must be in context |
| | $H_0$: P(on time)=0.92<br>$H_1$: P(on time)<0.92 | **B1** | Both.<br>Allow '$p$' or $\pi$ |
| | $1 - \left( {}^{20}C_{17} \times 0.92^{17} \times 0.08^3 + {}^{20}C_{18} \times 0.92^{18} \times 0.08^2 + 20 \times 0.92^{19} \times 0.08 + 0.92^{20} \right)$ | **M1** | Allow one end error<br>Must have 1 – … |
| | =0.0706 (3 sf) | **A1** | |
| | Compare with 0.05 | **M1** | Valid comparison needed |
| | No evidence that percentage less than 92% | **A1FT** | OE<br>No contradictions.<br><br>Method using normal approximation:<br>If the first B1B1 is earned then:<br>$\text{CV} - 1.566 \left( \text{from} \dfrac{16.5 - 20 \times 0.92}{\sqrt{20 \times 0.92 \times 0.08}}, \text{with continuity correction} \right)$<br>**or**<br>CV=1.978 (without continuity correction)<br><br>comp $z$=1.645<br>No evidence that % decreased (1.566) or evidence that % decreased (1.978) is awarded **SC2** after B marks |
| | | **6** | |

| Question | Answer | Marks | Guidance |
|---|---|---|---|
| 5(i) | Po(3) | **B1** | SOI |
| | $e^{-3}\left(\frac{3^3}{3!}+\frac{3^4}{4!}+\frac{3^5}{5!}\right)$ | **M1** | Allow one or two extra terms (2 or 6 or both) |
| | 0.493 (3 sf) | **A1** | |
| | | **3** | |
| 5(ii) | A correct equation from $P(0)=P(2)$ $\left(\text{leading to } 1=\frac{\lambda^2}{2}\right)$ | **M1** | |
| | $\lambda=\sqrt{2}$ or 1.41 (3 sf) | **A1** | CWO |
| | | **2** | |

| Question | Answer | Marks | Guidance |
|---|---|---|---|
| 5(iii)(a) | Correct inequality $\left(\text{leading to } \frac{5.2^n}{n!} < \frac{5.2^{n+1}}{(n+1)!}\right)$ | **B1** | |
| | | **1** | |
| 5(iii)(b) | $n+1 < 5.2$ or $1 < \frac{5.2}{n+1}$ | **M1** | Simplify to a stage without exponentials, powers or factorials. |
| | Largest $n$ is 4 | **A1** | |
| | | **2** | |

| Question | Answer | Marks | Guidance |
|---|---|---|---|
| 6(i) | $k\int_0^3 \left(3x - x^2\right) \mathrm{d}x = 1$ | **M1** | Attempt to integrate f($x$) and = 1 |
| | $k\left[\frac{3}{2}x^2 - \frac{x^3}{3}\right]_0^3$<br>$k\left(\frac{27}{2} - \frac{27}{3}\right) = 1$ | **A1** | Correct integral and limits |
| | $k = \frac{2}{9}$ | **A1** | AG<br>No errors seen |
| | | **3** | |

| Question | Answer | Marks | Guidance |
|---|---|---|---|
| 6(ii) | $\frac{2}{9}\int_1^2\left(3x-x^2\right)\mathrm{d}x = \frac{2}{9}\left[\frac{3}{2}x^2-\frac{x^3}{3}\right]_1^2 = \frac{2}{9}\times\left(6-\frac{8}{3}-\frac{3}{2}+\frac{1}{3}\right)$ | **M1** | Attempt to integrate f($x$) d$x$ with limits 1 and 2<br>OE |
| | $\frac{13}{27}$ or 0.481 (3 sf) | **A1** | |
| | | **2** | |
| 6(iii) | $y = 3x - x^2$ symmetrical about $x = \frac{3}{2}$ | **M1** | Attempt $\frac{2}{9}\int_0^3(3x^2-x^3)\,\mathrm{d}x$ |
| | E($X$)= $\frac{3}{2}$ | **A1** | |
| | $\frac{2}{9}\int_0^3(3x^3-x^4)\,\mathrm{d}x$ | **M1** | Attempt to integrate $x^2$f($x$) |
| | $=\frac{2}{9}\left[\frac{3x^4}{4}-\frac{x^5}{5}\right]_0^3\left(=\frac{2}{9}\times\frac{243}{20}=\frac{27}{10}\right)$<br>$\frac{'27'}{10}-\left(\frac{'3'}{2}\right)^2$ | **M1** | Subtract their (E($X$))$^2$ from their integral $x^2$f($x$) with correct limits substituted |
| | $\frac{9}{20}$ or 0.45 | **A1** | |
| | | **5** | |

| Question | Answer | Marks | Guidance |
|---|---|---|---|
| 7(i) | $H_0$: Pop mean=546<br>$H_1$: Pop mean>546 | **B1** | Both. Allow just $\mu$, but not just 'mean' |
| | $\frac{581-546}{\frac{120}{\sqrt{40}}}$ | **M1** | Standardising. Need $\frac{120}{\sqrt{40}}$ |
| | =1.845 allow 1.844 | **A1** | Allow 1.84 or 1.85 AWRT |
| | 1.845<1.96 | **M1** | OE. Or area comparison 0.0325>0.025 or large probabilities |
| | No evidence that mean weekly income has increased | **A1FT** | No contradictions.<br>If $H_1$: ≠, and 2.241 used, max B0M1A1M1A0 |
| | | **5** | |
| 7(ii) | $\frac{a-546}{\frac{120}{\sqrt{40}}}=1.96$ | **M1** | Standardise to find $a$. Need $\frac{120}{\sqrt{40}}$ **and** 546 **and** a value of $z$ |
| | $a$ = 583.19 | **A1** | Allow 583 to 3sf |
| | $\frac{'583.19'-595}{\frac{120}{\sqrt{40}}}(=-0.622)$ | **M1** | Standardise. Need $\frac{120}{\sqrt{40}}$ and 595 |
| | ϕ('–0.622')=1 – ϕ('0.622') | **M1** | Consistent area |
| | 0.267 | **A1** | |
| | | **5** | |