Cambridge International AS Level

Cambridge Assessment International Education
Cambridge International Advanced Subsidiary Level

MATHEMATICS **9709/23**

Paper 2 **October/November 2017**

MARK SCHEME

Maximum Mark: 50

Published

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

Cambridge International will not enter into discussions about these mark schemes.

Cambridge International is publishing the mark schemes for the October/November 2017 series for most Cambridge IGCSE®, Cambridge International A and AS Level components and some Cambridge O Level components.

® IGCSE is a registered trademark.

© UCLES 2017

Mark Scheme Notes

Marks are of the following three types:

M Method mark, awarded for a valid method applied to the problem. Method marks are not lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. Correct application of a formula without the formula being quoted obviously earns the M mark and in some cases an M mark can be implied from a correct answer.

A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated method mark is earned (or implied).

B Mark for a correct result or statement independent of method marks.

- When a part of a question has two or more 'method' steps, the M marks are generally independent unless the scheme specifically says otherwise; and similarly when there are several B marks allocated. The notation DM or DB (or dep*) is used to indicate that a particular M or B mark is dependent on an earlier M or B (asterisked) mark in the scheme. When two or more steps are run together by the candidate, the earlier marks are implied and full credit is given.

- The symbol FT implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A or B marks are given for correct work only. A and B marks are not given for fortuitously "correct" answers or results obtained from incorrect working.

- Note: B2 or A2 means that the candidate can earn 2 or 0.
  B2/1/0 means that the candidate can earn anything from 0 to 2.

  The marks indicated in the scheme may not be subdivided. If there is genuine doubt whether a candidate has earned a mark, allow the candidate the benefit of the doubt. Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored.

- Wrong or missing units in an answer should not lead to the loss of a mark unless the scheme specifically indicates otherwise.

- For a numerical answer, allow the A or B mark if a value is obtained which is correct to 3 s.f., or which would be correct to 3 s.f. if rounded (1 d.p. in the case of an angle). As stated above, an A or B mark is not given if a correct numerical answer arises fortuitously from incorrect working. For Mechanics questions, allow A or B marks for correct answers which arise from taking *g* equal to 9.8 or 9.81 instead of 10.

© UCLES 2017

The following abbreviations may be used in a mark scheme or used on the scripts:

AEF/OE Any Equivalent Form (of answer is equally acceptable) / Or Equivalent

AG Answer Given on the question paper (so extra checking is needed to ensure that the detailed working leading to the result is valid)

CAO Correct Answer Only (emphasising that no 'follow through' from a previous error is allowed)

CWO Correct Working Only – often written by a 'fortuitous' answer

ISW Ignore Subsequent Working

SOI Seen or implied

SR Special Ruling (detailing the mark to be given for a specific wrong solution, or a case where some standard marking practice is to be varied in the light of a particular circumstance)

Penalties

MR –1 A penalty of MR –1 is deducted from A or B marks when the data of a question or part question are genuinely misread and the object and difficulty of the question remain unaltered. In this case all A and B marks then become 'follow through' marks. MR is not applied when the candidate misreads his own figures – this is regarded as an error in accuracy. An MR –2 penalty may be applied in particular cases if agreed at the coordination meeting.

PA –1 This is deducted from A or B marks in the case of premature approximation. The PA –1 penalty is usually discussed at the meeting.

© UCLES 2017

Question	Answer	Marks	Guidance
1	Use subtraction or addition property of logarithms	***M1**	
	Obtain $\frac{3x+1}{x+2} = \mathrm{e}$ or equivalent with no presence of logarithm	**A1**	
	Use correct process to solve equation	**DM1**	
	Obtain $\frac{2\mathrm{e}-1}{3-\mathrm{e}}$ or exact equivalent	**A1**	
		4	

Question	Answer	Marks	Guidance
2	Use $\cos 2\theta = 2\cos^2\theta - 1$	**B1**	
	Obtain $10\cos^3\theta = 4$ or equivalent	**B1**	
	Use correct process to find at least one value of θ from equation of form $k_1\cos^3\theta = k_2$	**M1**	
	Obtain 42.5	**A1**	
	Obtain 317.5 and no others between 0 and 360	**A1**	
		5	

Question	Answer	Marks	Guidance
3	Take logarithms of both sides and apply power law	**M1**	Condone incorrect inequality signs until final answer. The first 6 marks are for obtaining the correct critical values.
	Obtain $2x < \frac{\ln 80}{\ln 1.3}$ or equivalent using $\log_{10}$	**A1**	
	Obtain $x = 8.35...$	**A1**	
	State or imply non-modulus inequality $(3x-1)^2 > (3x-10)^2$ or corresponding equation or linear equation $3x-1 = -(3x-10)$	**B1**	
	Attempt solution of inequality or equation (obtaining 3 terms when squaring each bracket or solving linear equation with signs of $3x$ different)	**M1**	
	Obtain $x = \frac{11}{6}$ or $x = 1.83...$	**A1**	
	Conclude $1.83 < x < 8.35$	**A1**	
		7	

Question	Answer	Marks	Guidance
4(a)	Obtain integrand of form $a\sec^2\theta + b$	**M1**	
	Obtain correct $5\sec^2\theta - 1$	**A1**	
	Integrate to obtain form $a\tan\theta + b\theta$	**M1**	
	Obtain $5\tan\theta - \theta + c$	**A1**	
		4	
4(b)	Obtain integral of form $k\ln(3x+1)$	***M1**	
	Apply limits and obtain $\frac{2}{3}\ln(3a+1) = \ln 16$	**A1**	
	Obtain equation with no presence of ln	**DM1**	
	Obtain 21	**A1**	
		4	

Question	Answer	Marks	Guidance
5(i)	Substitute $x = -2$ and equate to zero	***M1**	
	Substitute $x = \frac{1}{2}$ and equate to 40	***M1**	
	Obtain $-8a + 4b - 64 = 0$ and $\frac{1}{8}a + \frac{1}{4}b = \frac{23}{2}$ or equivalents	**A1**	
	Solve a pair of simultaneous equations for a or for b	**DM1**	Needs at least one of the two previous M marks
	Obtain $a = 12$ and $b = 40$	**A1**	
		5	
5(ii)	Attempt division by $(x + 2)$ or inspection at least as far as $kx^2 + mx$	**M1**	
	Obtain $12x^2 + 16x + 5$	**A1**	
	Conclude $(x + 2)(2x + 1)(6x + 5)$	**A1**	
		3	

Question	Answer	Marks	Guidance
6(i)	Obtain $\frac{dx}{dt} = 4e^{2t} + 4e^{t}$	**B1**	
	Use product rule to find $\frac{dy}{dt}$	**M1**	
	Obtain $\frac{dy}{dx} = \frac{5e^{2t} + 10te^{2t}}{4e^{2t} + 4e^{t}}$ or equivalent	**A1**	
	Equate first derivative of the form $\frac{ae^{2t} + bte^{2t}}{ce^{2t} + de^{t}}$ to zero and solve to find t	**M1**	
	Obtain $t = -\frac{1}{2}$ from completely correct work	**A1**	
	Obtain $(3.16, -0.92)$	**A1**	
		6	

© UCLES 2017

Question	Answer	Marks	Guidance
6(ii)	Identify $t = 0$	**B1**	
	Substitute $t = 0$ in expression for first derivative and find negative reciprocal	**M1**	
	Obtain $-\frac{8}{5}$ or equivalent	**A1**	
		3	

Question	Answer	Marks	Guidance
7(i)	Differentiate to obtain form $k_1x + k_2 + k_3\sin\frac{1}{2}x$	***M1**	
	Obtain correct $2x + 3 - \frac{5}{2}\sin\frac{1}{2}x$ and deduce or imply gradient at P is 3	**A1**	
	Equate first derivative to their -3 and rearrange	**DM1**	
	Obtain $x = \frac{5}{4}\sin\frac{1}{2}x - 3$	**A1**	
		4	
7(ii)	Consider sign of their $2x + 6 - \frac{5}{2}\sin\frac{1}{2}x$ at -4.5 and -4.0 or equivalent	**M1**	
	Complete argument correctly for correct expression with appropriate calculations	**A1**	
		2	
7(iii)	Use iteration formula correctly at least once	**M1**	
	Obtain final answer -4.11	**A1**	
	Show sufficient iterations to justify accuracy to 3 sf or show sign change in interval $(-4.115, -4.105)$	**A1**	
		3	

© UCLES 2017