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Cambridge International Advanced Subsidiary and Advanced Level

MARK SCHEME for the October/November 2014 series

9709 MATHEMATICS

9709/62 Paper 6, maximum raw mark 50

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

Cambridge will not enter into discussions about these mark schemes.

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Mark Scheme Notes

Marks are of the following three types:

M Method mark, awarded for a valid method applied to the problem. Method marks are not lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. Correct application of a formula without the formula being quoted obviously earns the M mark and in some cases an M mark can be implied from a correct answer.

A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated method mark is earned (or implied).

B Mark for a correct result or statement independent of method marks.

- When a part of a question has two or more "method" steps, the M marks are generally independent unless the scheme specifically says otherwise; and similarly when there are several B marks allocated. The notation DM or DB (or dep*) is used to indicate that a particular M or B mark is dependent on an earlier M or B (asterisked) mark in the scheme. When two or more steps are run together by the candidate, the earlier marks are implied and full credit is given.

- The symbol √ implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A or B marks are given for correct work only. A and B marks are not given for fortuitously "correct" answers or results obtained from incorrect working.

- Note: B2 or A2 means that the candidate can earn 2 or 0.
  B2/1/0 means that the candidate can earn anything from 0 to 2.

  The marks indicated in the scheme may not be subdivided. If there is genuine doubt whether a candidate has earned a mark, allow the candidate the benefit of the doubt. Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored.

- Wrong or missing units in an answer should not lead to the loss of a mark unless the scheme specifically indicates otherwise.

- For a numerical answer, allow the A or B mark if a value is obtained which is correct to 3 s.f., or which would be correct to 3 s.f. if rounded (1 d.p. in the case of an angle). As stated above, an A or B mark is not given if a correct numerical answer arises fortuitously from incorrect working. For Mechanics questions, allow A or B marks for correct answers which arise from taking g equal to 9.8 or 9.81 instead of 10.

The following abbreviations may be used in a mark scheme or used on the scripts:

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AEF Any Equivalent Form (of answer is equally acceptable)

AG Answer Given on the question paper (so extra checking is needed to ensure that the detailed working leading to the result is valid)

BOD Benefit of Doubt (allowed when the validity of a solution may not be absolutely clear)

CAO Correct Answer Only (emphasising that no "follow through" from a previous error is allowed)

CWO Correct Working Only – often written by a 'fortuitous' answer

ISW Ignore Subsequent Working

MR Misread

PA Premature Approximation (resulting in basically correct work that is insufficiently accurate)

SOS See Other Solution (the candidate makes a better attempt at the same question)

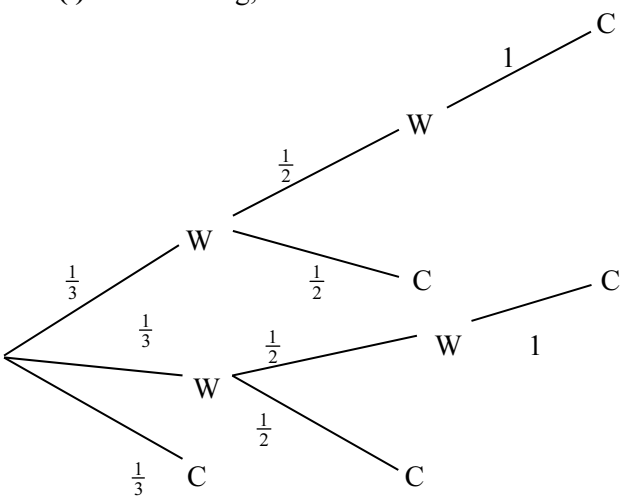
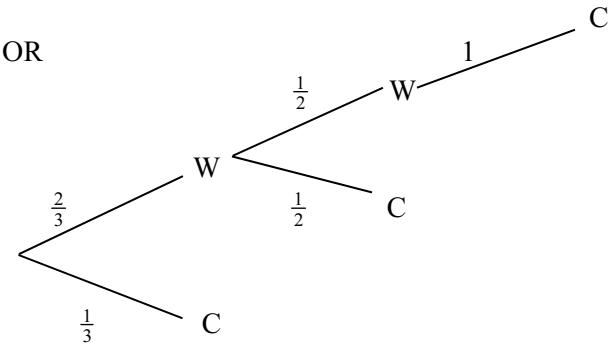
SR Special Ruling (detailing the mark to be given for a specific wrong solution, or a case where some standard marking practice is to be varied in the light of a particular circumstance)

Penalties

MR –1 A penalty of MR –1 is deducted from A or B marks when the data of a question or part question are genuinely misread and the object and difficulty of the question remain unaltered. In this case all A and B marks then become "follow through √" marks. MR is not applied when the candidate misreads his own figures – this is regarded as an error in accuracy. An MR –2 penalty may be applied in particular cases if agreed at the coordination meeting.

PA –1 This is deducted from A or B marks in the case of premature approximation. The PA –1 penalty is usually discussed at the meeting.

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1	$^{48}C_{43}$	B1	48 seen in a single term combination oe
		B1	43 or 5 seen in a single term combination oe Both can be mult by integer $k \geqslant 1$
	= 1712304 (1710000)	B1 **3**	Correct final answer
2	**(i)** 6! ×5!	B1	6! oe seen multiplied by integer $k \geqslant 1$
		B1	5! oe seen multiplied by integer $k \geqslant 1$
	= 86400	B1 **3**	Correct final answer
	(ii) 6! × 7 × 6 × 5 × 4	B1	6! seen mult by integer $k \geqslant 1$
		B1	Mult by $^7P_4$ oe
	= 604800	B1 **3**	Correct final answer
3	**(i)** 1 1 1 2 or 1 1 2 1 or 1 2 1 1 or 2 1 1 1	M1	One of 1 1 1 2 seen
	Prob = $\frac{1}{6}\times\frac{1}{6}\times\frac{1}{6}\times\frac{1}{6}\times 4$	M1	Mult a prob by 4 or $(\frac{1}{6})^4 \times$ integer $k \geqslant 1$ seen
	$= \frac{1}{324}$ (0.00309)	A1 **3**	Correct answer
	(ii) $P(1,2) = {}^7C_1 \times (1/324)\,(323/324)^6 + {}^7C_2(1/324)^2(323/324)^5$	M1	Bin term $^7C_x p^x (q)^{7-x}$, $0.99 \leqslant p + q \leqslant 1$
		M1	Using their p from **(i)** in a bin term
		M1	Correct unsimplified answer
	= 0.0214	A1 **4**	Correct answer
4	**(i)** W = wrong, C = correct		
		M1	3 branches first qn and 2 by 2 for second qn only
		M1	One branch twice for third qn or two branches twice with 0 and 1 seen on branches
		B1	Any two of $\frac{1}{3}$, $\frac{1}{2}$ and 1 seen as probs
		A1 **4**	Probs all correct and sensible labels NB SR for 4 outcomes instead of 3, M1 B1 only
	OR	M1	2 branches first qn and 1 by 2 for second qn only
		M1	One branch once for third qn or two branches with 0 and 1 seen on branches
		B1	Any two of $\frac{1}{3}$ or $\frac{2}{3}$, $\frac{1}{2}$ and 1 seen as probs
		A1	Probs all correct and sensible labels

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(ii)

x	1	2	3
Prob	$\frac{1}{3}$	$\frac{1}{3}$	$\frac{1}{3}$

P(1) = P(C) say $= \frac{1}{3}$

P(2) = P(WC) = $\frac{1}{6}$ P(WC) = $\frac{1}{6}$ total P (2) = $\frac{1}{3}$

P(3) = P(WWC) = $\frac{1}{6}$ P(WWC) = $\frac{1}{6}$ total P(3) = $\frac{1}{3}$

$E(X) = 1 \times \frac{1}{3} + 2 \times \frac{1}{3} + 3 \times \frac{1}{3} = 2$

B1

B1

B1

B1√ **4**

1, 2, 3 seen only oe

2 correct probs

3 correct probs

Correct answer ft their probs provided $0.999 \leqslant \Sigma p \leqslant 1$

5 **(a)** **(i)** $P(x < 8) = P\left(z < \frac{8 - 7.15}{0.88}\right)$

$= \Phi(0.9659)$

$= 0.833$

M1

A1 **2**

Standardising ± , no cc no sq rt no sq

Correct answer

(ii) $z = 0.674$

$\frac{q - 7.15}{0.88} = 0.674$

$q = 7.74$

B1

M1

A1 **3**

Accept ± 0.674 or 0.675 only

Standardised eqn = ± their z-value, allow sq or sq rt if already penalised in **(i)**

Correct answer

(b) $P(Y > 4\mu) = P\left(z > \frac{4\mu - \mu}{(3\mu/2)}\right) = P(z > 2)$

$= 1 - 0.9772$

$= 0.0228$

M1

A1

A1 **3**

Standardising no sq rt, no cc, no sq, one variable

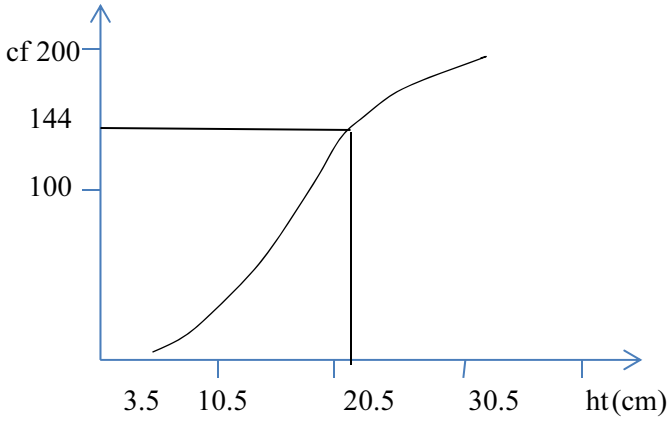
$z = \pm 2$ seen

correct ans SR B1 if made-up values used and 0.0228 obtained

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6 (i)

ht	<10.5	<15.5	<20.5	<25.5	<30.5
CF	22	54	132	172	200



B1 At least 4 CFs correct seen on graph

B1 Labels correct, i.e. all of ht, cm, cf

M1 Attempt at upper end points either 10 or 10.5 or 11 at least 4 upper end points

A1 **4** All correct, i.e. points joined up from (3.5, 0) to (10.5, 22)….to (30.5, 200) Straight lines or curve

(ii) 72% less, i.e. 144 less than ht h.
$h = 22.5$ cm

M1 144 **used** can be implied
A1 **2** single value in range 21 to 23 inclusive

(iii) var = $(7^2 \times 22 + 13^2 \times 32 + 18^2 \times 78 + 23^2 \times 40 + 28^2 \times 28)/200 - 18.39^2$
$= 74870/200 - 18.39^2$
$= 374.35 - 18.39^2$
$= 36.1579$

M1 Using mid points attempt 7 ± 0.5in correct var formula incl $-$ mean^2

B1 At least 4 correct midpoints

sd = 6.01

A1 **3** Correct ans

7 (i) P (4, 5, 6) = $(0.75)^4 (0.25)^4 \times {}^8C_4 + (0.75)^5 (0.25)^3 \times {}^8C_5 + (0.75)^6 (0.25)^2 \times {}^8C_6$

M1 Bin term $p^r(1-p)^{8-r} \times {}^8C_r$ seen any p

M1 Correct unsimplified answer

$= 0.606$

A1 **3** Correct ans

(ii) $np = 160 \times 0.75 = 120$ $npq = 30$

B1 Unsimplified mean and var correct

$$P(>114) = P\left(z > \left(\frac{114.5 - 120}{\sqrt{30}}\right)\right)$$

M1 Standardising, need sq rt
M1 Cont correction either 114.5 or 113.5

$= P(z > -1.004)$

M1 Correct area consistent with their working

$= \Phi(1.004) = 0.842$

A1 **5** Correct ans

(iii) np and nq both > 5

B1 **1** Need both

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