CAMBRIDGE
International Education

Cambridge International A Level

MATHEMATICS **9709/32**

Paper 3 Pure Mathematics 3 **May/June 2025**

MARK SCHEME

Maximum Mark: 75

Published

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

Cambridge International will not enter into discussions about these mark schemes.

Cambridge International is publishing the mark schemes for the May/June 2025 series for most Cambridge IGCSE, Cambridge International A and AS Level components, and some Cambridge O Level components.

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Generic Marking Principles

These general marking principles must be applied by all examiners when marking candidate answers. They should be applied alongside the specific content of the mark scheme or generic level descriptions for a question. Each question paper and mark scheme will also comply with these marking principles.

GENERIC MARKING PRINCIPLE 1:
Marks must be awarded in line with:

- the specific content of the mark scheme or the generic level descriptors for the question
- the specific skills defined in the mark scheme or in the generic level descriptors for the question
- the standard of response required by a candidate as exemplified by the standardisation scripts.

GENERIC MARKING PRINCIPLE 2:
Marks awarded are always **whole marks** (not half marks, or other fractions).

GENERIC MARKING PRINCIPLE 3:
Marks must be awarded **positively**:

- marks are awarded for correct/valid answers, as defined in the mark scheme. However, credit is given for valid answers which go beyond the scope of the syllabus and mark scheme, referring to your Team Leader as appropriate
- marks are awarded when candidates clearly demonstrate what they know and can do
- marks are not deducted for errors
- marks are not deducted for omissions
- answers should only be judged on the quality of spelling, punctuation and grammar when these features are specifically assessed by the question as indicated by the mark scheme. The meaning, however, should be unambiguous.

GENERIC MARKING PRINCIPLE 4:
Rules must be applied consistently, e.g. in situations where candidates have not followed instructions or in the application of generic level descriptors.

GENERIC MARKING PRINCIPLE 5:
Marks should be awarded using the full range of marks defined in the mark scheme for the question (however; the use of the full mark range may be limited according to the quality of the candidate responses seen).

GENERIC MARKING PRINCIPLE 6:
Marks awarded are based solely on the requirements as defined in the mark scheme. Marks should not be awarded with grade thresholds or grade descriptors in mind.

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Mathematics-Specific Marking Principles

1 Unless a particular method has been specified in the question, full marks may be awarded for any correct method. However, if a calculation is required then no marks will be awarded for a scale drawing.

2 Unless specified in the question, non-integer answers may be given as fractions, decimals or in standard form. Ignore superfluous zeros, provided that the degree of accuracy is not affected.

3 Allow alternative conventions for notation if used consistently throughout the paper, e.g. commas being used as decimal points.

4 Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored (isw).

5 Where a candidate has misread a number or sign in the question and used that value consistently throughout, provided that number does not alter the difficulty or the method required, award all marks earned and deduct just 1 A or B mark for the misread.

6 Recovery within working is allowed, e.g. a notation error in the working where the following line of working makes the candidate's intent clear.

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Annotations guidance for centres

Examiners use a system of annotations as a shorthand for communicating their marking decisions to one another. Examiners are trained during the standardisation process on how and when to use annotations. The purpose of annotations is to inform the standardisation and monitoring processes and guide the supervising examiners when they are checking the work of examiners within their team. The meaning of annotations and how they are used is specific to each component and is understood by all examiners who mark the component.

We publish annotations in our mark schemes to help centres understand the annotations they may see on copies of scripts. Note that there may not be a direct correlation between the number of annotations on a script and the mark awarded. Similarly, the use of an annotation may not be an indication of the quality of the response.

The annotations listed below were available to examiners marking this component in this series.

Annotations

Annotation	Meaning
	More information required
	Accuracy mark awarded zero
	Accuracy mark awarded one
	Independent accuracy mark awarded zero
	Independent accuracy mark awarded one
	Independent accuracy mark awarded two
	Benefit of the doubt
	Blank Page
	Incorrect
Dep	Used to indicate DM0 or DM1

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Annotation	Meaning
DM1	Dependent on the previous M1 mark(s)
FT	Follow through
	Indicate working that is right or wrong
Highlighter	Highlight a key point in the working
ISW	Ignore subsequent work
J	Judgement
JU	Judgement
M0	Method mark awarded zero
M1	Method mark awarded one
M2	Method mark awarded two
MR	Misread
O	Omission or Other solution
Off-page comment	Allows comments to be entered at the bottom of the RM marking window and then displayed when the associated question item is navigated to.
On-page comment	Allows comments to be entered in speech bubbles on the candidate response.
PE	Judgment made by the PE
Pre	Premature approximation
SC	Special case
SEEN	Indicates that work/page has been seen

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Annotation	Meaning
SF	Error in number of significant figures
	Correct
TE	Transcription error
XP	Correct answer from incorrect working

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Mark Scheme Notes

The following notes are intended to aid interpretation of mark schemes in general, but individual mark schemes may include marks awarded for specific reasons outside the scope of these notes.

Types of mark

M Method mark, awarded for a valid method applied to the problem. Method marks are not lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. Correct application of a formula without the formula being quoted obviously earns the M mark and in some cases an M mark can be implied from a correct answer.

A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated method mark is earned (or implied).

B Mark for a correct result or statement independent of method marks.

DM or **DB** When a part of a question has two or more 'method' steps, the M marks are generally independent unless the scheme specifically says otherwise; and similarly, when there are several B marks allocated. The notation DM or DB is used to indicate that a particular M or B mark is dependent on an earlier M or B (asterisked) mark in the scheme. When two or more steps are run together by the candidate, the earlier marks are implied and full credit is given.

FT Implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A or B marks are given for correct work only.

- A or B marks are given for correct work only (not for results obtained from incorrect working) unless follow through is allowed (see abbreviation FT above).
- For a numerical answer, allow the A or B mark if the answer is correct to 3 significant figures or would be correct to 3 significant figures if rounded (1 decimal place for angles in degrees).
- The total number of marks available for each question is shown at the bottom of the Marks column.
- Wrong or missing units in an answer should not result in loss of marks unless the guidance indicates otherwise.
- Square brackets [ ] around text or numbers show extra information not needed for the mark to be awarded.

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Abbreviations

AEF/OE	Any Equivalent Form (of answer is equally acceptable) / Or Equivalent
AG	Answer Given on the question paper (so extra checking is needed to ensure that the detailed working leading to the result is valid)
CAO	Correct Answer Only (emphasising that no 'follow through' from a previous error is allowed)
CWO	Correct Working Only
ISW	Ignore Subsequent Working
SOI	Seen Or Implied
SC	Special Case (detailing the mark to be given for a specific wrong solution, or a case where some standard marking practice is to be varied in the light of a particular circumstance)
WWW	Without Wrong Working
AWRT	Answer Which Rounds To

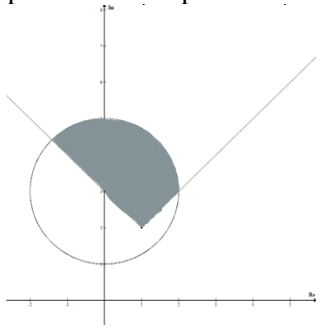
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Question	Answer	Marks	Guidance
1	Obtain a 3-term quadratic in e^x	***M1**	
	Obtain e.g. $3e^{2x} - 12e^x - 2 = 0$ or 3-term equivalent	**A1**	E.g. $3m^2 - 12m - 2 = 0$. '= 0' could be implied by subsequent working.
	Solve a 3-term quadratic to obtain a value for x or e^x	**DM1**	Need to get as far as a value for x or e^x.
	Obtain root $\frac{6+\sqrt{42}}{3}$ or 4.16…	**A1**	OE Ignore second root if seen.
	Obtain answer 1.426 only	**A1**	CAO, must be 3 d.p. 0/5 for answer with no working. Second root must be rejected if seen.
		5	

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Question	Answer	Marks	Guidance
2(a)	Find the first two terms of the expansion of $(1-2x)^{-\frac{3}{2}}$	**B1**	
	Obtain correct third term $\frac{-\frac{3}{2}\left(-\frac{3}{2}-1\right)}{2!}(-2x)^2$ or $\frac{-\frac{3}{2}\left(-\frac{3}{2}-1\right)}{2!}(2x)^2$	**B1**	$\frac{15}{2}x^2$ Ignore extra terms.
	Multiply *their* 3 term expansion $a+bx+cx^2$ by $(6-x)$ obtaining all necessary terms	**M1**	$6+18x+45x^2-x-3x^2....$ Ignore extra terms.
	$6 + 17x + 42x^2$	**A1**	Ignore extra terms. Allow with the terms in any order.
		4	
2(b)	$\lvert x\rvert < \frac{1}{2}$ or $-\frac{1}{2} < x < \frac{1}{2}$ or (-0.5, 0.5) or]-0.5, 0.5[	**B1**	OE B0 for an ambiguous statement. Must be strict inequality.
		1	

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Question	Answer	Marks	Guidance
3	Show a circle centre (0, 3)	**B1**	Allow for a circle in the correct place even if their scales require an ellipse. '3' marked on the axis, centre implied by vertical intercepts or dashes to indicate a scale.
	Show a circle with radius 2	**B1FT**	FT centre not at the origin. Consistent with *their* scale if they have unequal scales on the axes.
	Show the point representing (1, 2)	**B1**	Position can be implied provided there is some indication of scale, e.g. numbers or marks on the axes.
	Show correct half-lines from (1, 2), one at an angle of $\frac{1}{4}\pi$ and the other at an angle of $\frac{3}{4}\pi$	**B1FT**	FT from *their* (1, 2) not at the origin. Correct lines can imply previous B1. Half-lines must be intended to be 'symmetrical'. Angles consistent with *their* scale: correct lines need to pass very close to (0, 3) and (2, 3).
	Shade the correct region	**B1**	Dependent on all previous marks. 
		5	

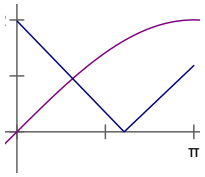
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Question	Answer	Marks	Guidance
4	Use correct trigonometric formulae to form an equation in $\tan x$ only, or an equation in terms of $\sin x$ and $\cos x$ only e.g. $\dfrac{3}{\tan x} - 4\left(\dfrac{1-\tan^2 x}{2\tan x}\right) = 3$ $\dfrac{3}{\tan x} - \dfrac{4}{\frac{2\tan x}{1-\tan^2 x}} = 3$ $3\dfrac{\cos x}{\sin x} - 4\dfrac{\cos^2 x - \sin^2 x}{2\sin x\cos x} = 3$ $3\cot x - 4\left(\dfrac{\cot^2 x - 1}{2\cot x}\right) = 3$	***M1**	Condone one slip in manipulating the original equation provided correct trig formulae used.
	Obtain a correct horizontal equation, in $\tan x$ or in $\cos x$ and $\sin x$, in any form	**A1**	E.g. $3 - (2 - 2\tan^2 x) = 3\tan x$ or $2\sin^2 x - 3\sin x\cos x + \cos^2 x = 0$.
	Reduce equation to a 3-term quadratic Allow if they square both sides and obtain a quartic in $\sin x$ or $\cos x$	**A1**	E.g. $2\tan^2 x - 3\tan x + 1 = 0$, $2\sin^2 x - 3\sin x\cos x + \cos^2 x = 0$. Allow if they leave the equation as a cubic with a factor of $\tan x$ and go on to give the correct solutions to the quadratic.
	Solve a 3-term quadratic to obtain a value for x The quadratic could be arrived at from a correct cubic Not available if they have an incorrect cubic with an incorrect quadratic factor.	**DM1**	If the initial equation is correct, then M1 is implied by a correct solution.
	Obtain one answer, e.g. (x =) 45°	**A1**	
	Obtain a second answer, e.g. AWRT (x =) 26.6° and no other in the given interval, e.g. $x = 0$	**A1**	Ignore answers outside the given interval.
		6	

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Question	Answer	Marks	Guidance
5	Square $x + iy$ and equate real and imaginary parts to -1 and $-4\sqrt{5}$ respectively	***M1**	
	Obtain equations $x^2 - y^2 = -1$ and $2xy = -4\sqrt{5}$ from *their* expansion	**A1**	
	Working from two equations in two unknowns, eliminate one variable and find an equation in the other	**DM1**	Do not condone incorrect algebra, e.g. $x = -2\sqrt{5}y$.
	Obtain $x^4 + x^2 - 20 = 0$ or $y^4 - y^2 - 20 = 0$	**A1**	Accept 3-term equivalents. Condone missing "= 0" if implied by subsequent working.
	Obtain answers $\pm\left(2 - \sqrt{5}\mathrm{i}\right)$ and no others	**A1**	Must state the square roots, not x and y separately, and not coordinates. Do not allow $\sqrt{4}$ in place of 2. A0 if there are additional incorrect solutions. No working seen scores 0/5.
		5	

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Question	Answer	Marks	Guidance
6(a)	Sketch a relevant graph for $0 < x < \pi$ For $y = \lvert x - 2 \rvert$ graph should be symmetrical and have correct intercepts on the axes For $y = 2\sin\frac{1}{2}x$, graph should pass through the origin, have correct curvature and max $y = 2$ when $x = \pi$	**B1**	 Ignore anything outside $0 < x < \pi$. Ignore what happens in $y < 0$.
	Sketch second relevant graph and confirm root. The vertex of the modulus graph in roughly correct position relative to π and/or $\frac{1}{2}\pi$ If no mark on the graph, check to see if they have written something below the graph.	**B1**	Needs to mark intersection with a dot, a cross, or say roots at points of intersection, OE. If the intersection is highlighted in some way, then they do not need to make a comment.
			SC A sketch $y = x - 2$ **and** $y = \pm 2\sin\frac{1}{2}x$ (above and below the x-axis) scores B1. A clear indication of the root scores second B1.
		2	

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Question	Answer	Marks	Guidance
6(b)	Calculate the values of a relevant expression or pair of expressions at $x = 1$ and $x = 1.5$ e.g. $f(x) = \lvert x - 2\rvert - 2\sin\frac{1}{2}x$ $f(1) = 0.0411\ldots > 0$ $f(1.5) = -0.863\ldots < 0$ e.g. $f(x) = (x-2)^2 - 4\sin^2\left(\frac{1}{2}x\right) \Rightarrow f(1) = 0.0806..., f(1.5) = -1.60...$	**M1**	Or comparing $\lvert x - 2\rvert$ and $2\sin\frac{1}{2}x$. Using 1: $\lvert x - 2\rvert = 1,\ 2\sin\frac{1}{2}x = 0.958\ldots$ $\Rightarrow 1 > 0.958\ldots$ Using 1.5: $\lvert x - 2\rvert = 0.5\ 2\sin\frac{1}{2}x = 1.36\ldots$ $\Rightarrow 0.5 < 1.36\ldots$ Need all values but condone one error. If the solution involves 4 values, the pairing must be clear. Embedded values are not sufficient, e.g. $f_1(1) = \ldots$ and $f_2(1) = \ldots$ etc. M0 if working in degrees (gives 0.98… and 0.47… if using $f(x) = 0$). Allow if working on a smaller interval.
	Complete the argument correctly with correct calculated values	**A1**	Values correct. They must have a conclusion in words or symbols, but they do not need to say that the function is continuous. A correct statement with correct inequalities is sufficient.
		2	

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Question	Answer	Marks	Guidance
6(c)	Use the iterative process correctly at least once starting at 1.03 (get as far as 1.0281)	**M1**	M0 if working in degrees.
	Obtain final answer 1.02	**A1**	No working seen at all scores 0/3.
	Show sufficient iterations to 4 d.p. to justify 1.02 to 2 d.p. or show there is a sign change in the interval (1.015, 1.025) (or a smaller interval containing the root)	**A1**	1.03, 1.0149, 1.0281, 1.0166, 1.0266, 1.0179, 1.0255, 1.0189, 1.0246 Incorrect starting point is M0. Once the convergence is established ISW.
		3	

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Question	Answer	Marks	Guidance
7(a)	State $R = 25$	**B1**	From correct work. BOD if correct value follows use of *their α,* but not if a decimal approximation to R is seen first.
	Use correct trig formula to find α, e.g. $\alpha = \tan^{-1}\left(\frac{7}{24}\right)$	**M1**	If $\cos\alpha = 24$ and $\sin\alpha = 7$ seen, then M0 A0.
	Obtain $\alpha = 0.2838$	**A1**	CAO
		3	
7(b)	$\cos^{-1}\left(\frac{24.5}{25}\right)$	**B1 FT**	Can be implied by $\pm 0.2(0033\ldots)$, or by $\frac{1}{3}x = 0.08...$ or $0.48...$ or a correct value of x following M1. FT *their R* from **(a)**. Allow B1 if $\cos^{-1}\left(\frac{24.5}{R}\right)$ is not evaluated, provided $R \geq 24.5$.
	Carry out a complete correct method to find a value of x Sight of a correct equation using **(a)** is needed, e.g. $\cos\left(\frac{1}{3}x - 0.2838\right) = 0.98$ OE	**M1**	Need some method shown, but might not show interim values if working on a calculator. Incorrect answers and insufficient evidence scores M0.
	Obtain answer ($x =$) 1.45	**A1**	AWRT Need 3 sf or better.
	Obtain ($x =$) 0.250 or ($x =$) 0.251, and no other in the interval	**A1**	AWRT Ignore answers outside the given interval.
		4	

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Question	Answer	Marks	Guidance
8	Separate variables correctly	**B1**	$\int \frac{1}{4x+3}\,\mathrm{d}x = \int \frac{\cos 2\theta}{\sin 2\theta}\,\mathrm{d}\theta$ Can be implied by obtaining both correct integrals.
	Obtain term $\frac{1}{4}\ln(4x+3)$	**B1**	OE or $\frac{1}{4}\ln\left(x+\frac{3}{4}\right)$.
	Obtain term of the form $A\ln(\sin 2\theta)$	**M1**	Or $A\ln(k\sin 2\theta)$ OE, e.g. $P\ln a\sin\theta + Q\ln b\cos\theta$ from using the $\tan 2\theta$ formula. Or expanding $\cos 2\theta$ as $\cos^2\theta - \sin^2\theta$.
	Obtain term $\frac{1}{2}\ln(\sin 2\theta)$	**A1**	OE Correct in any form, e.g. $\frac{1}{2}\ln a\sin\theta + \frac{1}{2}\ln b\cos\theta$.
	Use $x = 0$ when $\theta = \frac{1}{12}\pi$ to evaluate a constant or as limits in a solution containing terms of the form $\ln(\sin 2\theta)$ and $\ln(4x+3)$ c = ... seen or implied	**M1**	E.g. $c = \frac{1}{4}\ln 3 - \frac{1}{2}\ln\sin\left(\frac{1}{6}\pi\right)$ $\frac{1}{4}\ln(4x+3) - \frac{1}{4}\ln 3 = \frac{1}{2}\ln(\sin 2\theta) - \frac{1}{2}\ln\frac{1}{2}$. Note that the constant may be expressed as a logarithm
	Obtain correct answer in any form with the trigonometry evaluated	**A1**	E.g. $\frac{1}{4}\ln(4x+3) = \frac{1}{2}\ln(\sin 2\theta) + \frac{1}{4}\ln 12$ $\frac{1}{4}\ln(4x+3) = \frac{1}{2}\ln(\sin 2\theta) + 0.621$ $\frac{1}{4}\ln\frac{4x+3}{3} = \frac{1}{2}\ln(2\sin 2\theta)$
	Obtain final answer $x = \frac{12\sin^2 2\theta - 3}{4}$	**A1**	OE Allow $\frac{\mathrm{e}^{2.48\ldots}\sin^2 2\theta - 3}{4}$. Allow 2.48. Allow $x = \frac{1}{4}\left(\mathrm{e}^{2\ln(\sin 2\theta)+2.48\ldots} - 3\right)$.
		7	

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Question	Answer	Marks	Guidance
9(a)	Carry out a correct method for finding a vector equation for the line through A and B	**M1**	A complete method. Can be working from any point on AB.
	Obtain $\mathbf{r} = \begin{pmatrix} 1 \\ -4 \\ 2 \end{pmatrix} + \lambda \begin{pmatrix} -3 \\ 5 \\ 1 \end{pmatrix}$	**A1**	OE Must have $\mathbf{r} = \ldots$ not $l = \ldots$. Accept $\mathbf{r}_{AB} = \ldots$ Accept $\boldsymbol{R} = \ldots$.
		2	
9(b)	Obtain a direction vector for $\overrightarrow{AC} = \begin{pmatrix} 1 \\ 7 \\ 3 \end{pmatrix}$	**B1**	OE Or $\overrightarrow{CA}$.
	Carry out correct process for evaluating the scalar product of $\overrightarrow{AB}$ and $\overrightarrow{AC}$ or $\overrightarrow{BA}$ and $\overrightarrow{CA}$	**M1**	$-3\times1+5\times7+1\times3=35$ Allow for correct answer and no working seen.
	Using the correct process for the moduli, divide their scalar product by the product of the moduli	**M1**	Independent M0M1 is possible. ISW finding the angle.
	Obtain $(\cos BAC =) \sqrt{\frac{35}{59}}$ or exact simplified equivalent	**A1**	From correct working. The answer needs to come from using a scalar product. Accept $\frac{35}{\sqrt{2065}}$ or $\frac{35}{\sqrt{35}\sqrt{59}}$ or $\frac{\sqrt{2065}}{59}$ $\theta = \cos^{-1}\sqrt{\frac{35}{59}}$ without a statement of $\cos BAC$ scores A0. ISW finding the angle.
		4	

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Question	Answer	Marks	Guidance
9(c)	Use area $= \frac{1}{2}\left\|\overrightarrow{AB}\right\|\left\|\overrightarrow{AC}\right\|\sin BAC$ with *their* $\left\|\overrightarrow{AB}\right\|\left\|\overrightarrow{AC}\right\|$	**M1**	For "hence", must be using the angle at A. Need not substitute for the trigonometry. Accept any equivalent form for *their* $\sin BAC$.
	Use $\sin x = \sqrt{1-\cos^2 x}$ or an equivalent exact method with *their* $\cos x$ (< 1) to obtain an exact value for $\sin x$ $\frac{1}{2}\sqrt{35}\sqrt{59}\sqrt{1-\frac{35^2}{35\times 59}} = \frac{1}{2}\sqrt{35}\sqrt{59}\frac{\sqrt{840}}{\sqrt{35}\sqrt{59}}$	**M1**	NB: These two M marks are independent. Might not quote the formula. Could draw a triangle and use Pythagoras, which is equivalent. $\sin x = \sqrt{\frac{24}{59}}$ $\sin\left(\cos^{-1}\sqrt{\frac{35}{59}}\right)$ is allowed for the first M1, but not for the second.
	Obtain answer $\sqrt{210}$ from correct working	**A1**	Accept simplified equivalent exact forms, e.g. $\frac{1}{2}\sqrt{840}$. Watch out for fortuitous answers from negative value of the cosine. Do not accept an answer coming from $\sin\left(\cos^{-1}\sqrt{\frac{35}{59}}\right)$ with no evidence of the method of evaluation. The answer needs to come from using angle BAC.
		3	

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Question	Answer	Marks	Guidance
10(a)	Obtain quotient $\frac{1}{4}$	**B1**	Could be found by using long division or by writing $x^2 = q\left(1+4x^2\right)+r$ and comparing coefficients: $1 = 4q$, $0 = q + r$.
	Obtain remainder $-\frac{1}{4}$	**B1**	Allow B1B1 if implied by correct division and no further working, but do not ISW. Allow for a correct statement of the identity, but not for an incorrect statement of the remainder.
		2	

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Question	Answer	Marks	Guidance
10(b)	Commence integration by parts and reach $Ax^2 \tan^{-1} 2x \pm \int x^2 \frac{B}{C+Dx^2} \mathrm{d}x$	***M1**	OE
	Obtain $\frac{1}{2}x^2 \tan^{-1} 2x - \int \frac{x^2}{1+4x^2} \mathrm{d}x$	**A1**	OE
	Integrate $\int \frac{x^2}{1+4x^2} \mathrm{d}x$ to obtain an expression of the form $p \tan^{-1} 2x + qx$	**DM1**	
	Complete integration and obtain $\frac{1}{2}x^2 \tan^{-1} 2x + \frac{1}{8}\tan^{-1} 2x - \frac{1}{4}x$	**A1 FT**	OE FT *their* constant quotient and remainder from **(a),** and $\frac{k}{8}\tan^{-1} 2x - \frac{k}{4}x$ from *their* $\frac{kx^2}{1+4x^2}$.
	Substitute limits correctly in an expression of the form $Fx^2 \tan^{-1} 2x + G\tan^{-1} 2x + Hx$	**DM1**	Need some evidence that they have considered the lower limit, e.g. sight of 0 in the working. No need to evaluate trigonometry. If in stages, then the 0 needs to be seen for each part.
	Obtain answer $\frac{1}{16}\pi - \frac{1}{8}$ or exact one- or two-term equivalent with trigonometry evaluated	**A1**	
		6	

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Question	Answer	Marks	Guidance
11(a)	Differentiate $\cos^2 x$ to obtain $-2\sin x\cos x$	**B1**	OE Could be stated as $-\sin 2x$.
	Use correct product rule	***M1**	With a '+' in the middle.
	Obtain derivative $-10\sin 2x\sin x\cos x+10\cos 2x\cos^2 x$	**A1**	OE
	Equate derivative to zero and obtain an equation in one trig function	**DM1**	Trigonometry formulas used need to be correct.
	Obtain $3\tan^2 x = 1$, $4\sin^2 x = 1$ or $4\cos^2 x = 3$ or $\cos 3x = 0$	**A1**	OE
	Obtain $x = \frac{1}{6}\pi$ only	**A1**	
	Alternative Method for the Question 11(a)		
	Use double angle formula to obtain $y = 10\sin x\cos^3 x$	**B1**	
	Use correct product rule	***M1**	
	Obtain derivative $10\cos^4 x - 30\sin^2 x\cos^2 x$	**A1**	OE
	Equate derivative to zero and obtain an equation in one trig function	**DM1**	Trigonometry formulas used need to be correct.
	Obtain $3\tan^2 x = 1$, $4\sin^2 x = 1$ or $4\cos^2 x = 3$ or $\cos 3x = 0$	**A1**	OE
	Obtain $x = \frac{1}{6}\pi$ only	**A1**	

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Question	Answer	Marks	Guidance
11(a)	**Alternative Method 2 for the Question 11(a)**		
	Use double angle formula to obtain $y = \frac{5}{2}\sin 2x(\cos 2x + 1)$	**B1**	
	Use double angle formula to obtain $y = \frac{5}{4}\sin 4x + \frac{5}{2}\sin 2x$	***M1**	
	Obtain derivative $5\cos 4x + 5\cos 2x$	**A1**	
	Equate derivative to zero and obtain an equation in $\cos 2x$	**DM1**	$2\cos^2 2x + \cos 2x - 1 = 0$
	Obtain $\cos 2x = \frac{1}{2}$ only	**A1**	
	Obtain $x = \frac{1}{6}\pi$ only	**A1**	
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Question	Answer	Marks	Guidance
11(b)	$\frac{\mathrm{d}u}{\mathrm{d}x} = -\sin x$	**B1**	SOI
	Reach an integral of the form $\int Au^3 \,\mathrm{d}u$	***M1**	OE The question requires use of the substitution method.
	Obtain $-10\int u^3 \mathrm{d}u$	**A1**	OE Ignore limits, but check order of limits if no minus sign.
	Substitute correct limits correctly in an expression of the form Cu^4 or $C\cos^4 x$	**DM1**	$u = 1$ and $u = \frac{\sqrt{2}}{2}$ $x = 0$ and $x = \frac{1}{4}\pi$ $-10\int_1^{\frac{1}{\sqrt{2}}} u^3 \mathrm{d}u$ or $10\int_{\frac{1}{\sqrt{2}}}^1 u^3 \mathrm{d}u$ Allow the correct answer from the correct integration and relevant limits to imply M1.
	Obtain answer $\frac{15}{8}$ or 1.875	**A1**	WWW ISW
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