Cambridge International AS & A Level

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**MATHEMATICS** **9709/62**

Paper 6 **May/June 2016**

MARK SCHEME

Maximum Mark: 50

**Published**

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

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**Mark Scheme Notes**

Marks are of the following three types:

M Method mark, awarded for a valid method applied to the problem. Method marks are not lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. Correct application of a formula without the formula being quoted obviously earns the M mark and in some cases an M mark can be implied from a correct answer.

A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated method mark is earned (or implied).

B Mark for a correct result or statement independent of method marks.

- When a part of a question has two or more "method" steps, the M marks are generally independent unless the scheme specifically says otherwise; and similarly when there are several B marks allocated. The notation DM or DB (or dep*) is used to indicate that a particular M or B mark is dependent on an earlier M or B (asterisked) mark in the scheme. When two or more steps are run together by the candidate, the earlier marks are implied and full credit is given.

- The symbol √ implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A or B marks are given for correct work only. A and B marks are not given for fortuitously "correct" answers or results obtained from incorrect working.

- Note: B2 or A2 means that the candidate can earn 2 or 0.
  B2/1/0 means that the candidate can earn anything from 0 to 2.

  The marks indicated in the scheme may not be subdivided. If there is genuine doubt whether a candidate has earned a mark, allow the candidate the benefit of the doubt. Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored.

- Wrong or missing units in an answer should not lead to the loss of a mark unless the scheme specifically indicates otherwise.

- For a numerical answer, allow the A or B mark if a value is obtained which is correct to 3 s.f., or which would be correct to 3 s.f. if rounded (1 d.p. in the case of an angle). As stated above, an A or B mark is not given if a correct numerical answer arises fortuitously from incorrect working. For Mechanics questions, allow A or B marks for correct answers which arise from taking *g* equal to 9.8 or 9.81 instead of 10.

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The following abbreviations may be used in a mark scheme or used on the scripts:

AEF Any Equivalent Form (of answer is equally acceptable)

AG Answer Given on the question paper (so extra checking is needed to ensure that the detailed working leading to the result is valid)

BOD Benefit of Doubt (allowed when the validity of a solution may not be absolutely clear)

CAO Correct Answer Only (emphasising that no "follow through" from a previous error is allowed)

CWO Correct Working Only – often written by a 'fortuitous' answer

ISW Ignore Subsequent Working

MR Misread

PA Premature Approximation (resulting in basically correct work that is insufficiently accurate)

SOS See Other Solution (the candidate makes a better attempt at the same question)

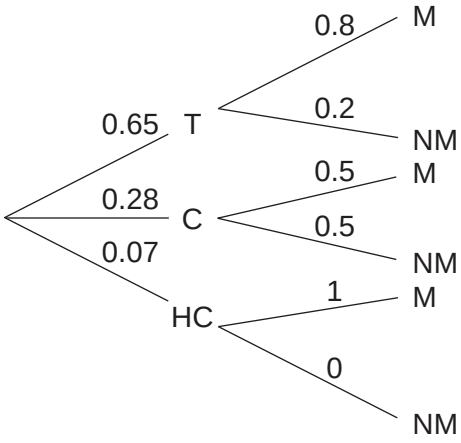
SR Special Ruling (detailing the mark to be given for a specific wrong solution, or a case where some standard marking practice is to be varied in the light of a particular circumstance)

**Penalties**

MR –1 A penalty of MR –1 is deducted from A or B marks when the data of a question or part question are genuinely misread and the object and difficulty of the question remain unaltered. In this case all A and B marks then become "follow through √" marks. MR is not applied when the candidate misreads his own figures – this is regarded as an error in accuracy. An MR –2 penalty may be applied in particular cases if agreed at the coordination meeting.

PA –1 This is deducted from A or B marks in the case of premature approximation. The PA –1 penalty is usually discussed at the meeting.

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| Qu | | Answer | Marks | Notes |
|---|---|---|---|---|
| 1 | (i) |  | **M1**<br><br>**A1** [2] | Correct shape with either one branch after HC or 2 branches with 0 prob seen correct Labelled and clear annotation<br><br>All probs correct |
| | (ii) | $P(C \mid \text{milk}) = \frac{P(coffee \cap milk)}{P(milk)}$<br>$= \frac{0.28 \times 0.5}{0.65 \times 0.8 + 0.28 \times 0.5 + 0.07(\times 1)}$<br>$= \frac{0.14}{0.73}$<br>$= 0.192$ | **M1**<br><br>**M1**<br><br>**A1** [3] | Attempt at P(coffee∩ milk)as a two-factor prod only seen as num or denom of a fraction<br><br>Summing appropriate three 2-factor products seen anywhere (can omit the 1)<br><br>Correct answer oe |
| 2 | (i) | 0.72 | **B1** [1] | |
| | (ii) | $np = 180 \times 0.72$, $npq = 180 \times 0.72 \times 0.28$<br>$X \sim N(129.6, 36.288)$<br>$P(x > 115) = P\left(z > \frac{115.5 - 129.6}{\sqrt{36.288}}\right)$<br>$= P(z > -2.341)$<br>$= 0.990$ | **B1**√<br>**M1**<br>**M1**<br>**M1**<br>**A1** [5] | $180 \times 0.72$, $180 \times 0.72 \times 0.28$ seen, their values or correct<br>Standardising ( ±) must have sq rt<br>cc either 115.5 or 114.5 seen<br>Correct area, Φ from final answer attempt fully correct method |
| 3 | (i) | <table><tr><td>$x$</td><td>1</td><td>2</td><td>3</td><td>4</td></tr><tr><td>P($x$)</td><td>$k$</td><td>$2k$</td><td>$3k$</td><td>$4k$</td></tr></table><br>$10k = 1$<br>$k = 1/10$ | **B1**<br><br>**M1**<br><br>**A1** [3] | Probability Distribution Table, either $k$ or correct numerical values<br>Summing probs involving $k$ to = 1, 3 or 4 terms |
| | (ii) | $E(X) = 1/10 + 4/10 + 9/10 + 16/10 = 3$<br>$\text{Var}(X) = 1/10 + 8/10 + 27/10 + 64/10 - 3^2$<br>$= 1$ | **B1**<br>**M1**<br>**A1** [3] | Correct mean<br>Correct method seen for var, their $k$ and $\mu$ |

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|---|---|---|---|---|
| **4** | **(i)** | $p = 0.66$ $X \sim$ B(15, 0.66)<br>P(at least 14) = P(14, 15) =<br>$^{15}C_{14}\,(0.66)^{14}(0.34) + (0.66)^{15}$<br><br>= 0.0171 | **M1**<br><br>**M1**<br><br>**A1** [3] | Bin term $^{15}C_x p^x(1-p)^{15-x}$ seen any $p$<br><br>Unsimplified correct expression for P(14,15) |
| | **(ii)** | $(0.87)^n < 0.04$<br><br><br><br>$n = 24$ | **M1**<br>**M1**<br><br><br>**A1** [3] | Eqn involving 0.87, power of n, 0.04 only<br>Solving by logs or trial and error(can be implied).<br>Must be exponential equation |
| **5** | **(i)** | Bronlea Rogate<br>6 3 0 4 5 7 7<br>7 4 3 1 0 1 3 5 6 8<br>8 7 5 4 2 1 2 3 3 6<br>3 2 3 4<br>5 4<br><br>Key 3\| 1 \| 5 represents 13 kph for Bronlea and 15 kph for Rogate | **B1**<br>**B1**<br>**B1**<br><br>**B1**<br><br>**B1** [5] | Correct single stem<br>Correct ordered leaves Bronlea<br>Correct ordered leaves Rogate<br><br>Correct overall shape<br><br>Single key must have both towns and units consistent with their values |
| | **(ii)** | median Bronlea = 23 km per hour<br>IQ range Rogate = 23 – 7<br><br>= 16 | **B1**<br>**M1**<br><br>**A1** [3] | Units not necessary<br>Subt their LQ <14 from their UQ>14 from Rogate leaf |
| | **(iii)** | Rogate is less windy than Bronlea | **B1** [1] | Not a comparison of a statistic but interpretation of information |
| **6** | **(i)** | $P(x > 10.2) = P\left(z > \frac{10.2-9.5}{1.3}\right)$<br>$= P(z > 0.53846)$<br>$= 1 - 0.7046$<br>$= 0.295$ | **M1**<br><br>**M1**<br><br>**A1** [3] | Standardising allow cc, sq rt, sq<br><br>1 – Φ final solution attempt |
| | **(ii)** | $z = -1.282$<br>$-1.282 = \frac{t-9.5}{1.3}$<br><br>$t = 7.83$ | **B1**<br><br>**M1**<br><br>**A1** [3] | ± rounding to 1.28 seen<br><br>Standardising correctly can be ± $z$ value here<br><br>Correct answer from $z = -1.282$ only |
| | **(iii)** | $P(x < 8.8) = 0.2954$ by symmetry<br>Days = 365×0.2954<br>= 107 or 108 | **B1**<br>**M1**<br>**A1** [3] | oe method, FT *their 0.2954 from (i)*<br>Mult a probability <1 by 365<br>Correct answer (no decimals) |
| **7** | **(a) (i)** | $\frac{10!}{2!3!} = 302400$ | **B1** [1] | Exact value only, isw rounding |

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| | | | |
|---|---|---|---|
| **(ii)** | e.g. *W******W*, **W******W, W******W** | **M1** | 8! Seen mult or alone. Cannot be embedded (arrangements of other 8 letters). |
| | $\frac{8!}{3!} \times 3$(for the Ws) | **M1** | Dividing by 3! (removing repeated L's) |
| | | **M1** | Mult by 3 (different W positions) may be sum of 3 terms |
| | = 20160 | **A1** [4] | |
| **(b)** | S(5) A(7) C(4)<br>1 3 2 : $5\times{}^7C_3\times{}^4C_2 = 1050$<br>1 4 1 : $5\times{}^7C_4\times 4 = 700$<br>2 3 1 : ${}^5C_2\times{}^7C_3\times 4 = 1400$<br>3 2 1 : ${}^5C_3\times{}^7C_2\times 4 = 840$<br>(Outcomes : Options) | **M1** | Mult 3 combinations, ${}^5C_x$, ${}^7C_y$, ${}^4C_z$ (not 5 x 7 x 4) |
| | | **A1** | 2 correct options unsimplified |
| | | **M1** | Summing only 3 or 4 correct outcomes involving combs or perms |
| | Total = 3990 | **A1** [4] | |

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