UNIVERSITY OF CAMBRIDGE INTERNATIONAL EXAMINATIONS

GCE Advanced Subsidiary Level and GCE Advanced Level

MARK SCHEME for the May/June 2012 question paper

for the guidance of teachers

9709 MATHEMATICS

9709/21 Paper 2, maximum raw mark 50

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes must be read in conjunction with the question papers and the report on the examination.

- Cambridge will not enter into discussions or correspondence in connection with these mark schemes.

Cambridge is publishing the mark schemes for the May/June 2012 question papers for most IGCSE, GCE Advanced Level and Advanced Subsidiary Level syllabuses and some Ordinary Level syllabuses.

UNIVERSITY of CAMBRIDGE
International Examinations

Mark Scheme Notes

Marks are of the following three types:

M Method mark, awarded for a valid method applied to the problem. Method marks are not lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. Correct application of a formula without the formula being quoted obviously earns the M mark and in some cases an M mark can be implied from a correct answer.

A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated method mark is earned (or implied).

B Mark for a correct result or statement independent of method marks.

- When a part of a question has two or more "method" steps, the M marks are generally independent unless the scheme specifically says otherwise; and similarly when there are several B marks allocated. The notation DM or DB (or dep*) is used to indicate that a particular M or B mark is dependent on an earlier M or B (asterisked) mark in the scheme. When two or more steps are run together by the candidate, the earlier marks are implied and full credit is given.

- The symbol √ implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A or B marks are given for correct work only. A and B marks are not given for fortuitously "correct" answers or results obtained from incorrect working.

- Note: B2 or A2 means that the candidate can earn 2 or 0.
  B2/1/0 means that the candidate can earn anything from 0 to 2.

  The marks indicated in the scheme may not be subdivided. If there is genuine doubt whether a candidate has earned a mark, allow the candidate the benefit of the doubt. Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored.

- Wrong or missing units in an answer should not lead to the loss of a mark unless the scheme specifically indicates otherwise.

- For a numerical answer, allow the A or B mark if a value is obtained which is correct to 3 s.f., or which would be correct to 3 s.f. if rounded (1 d.p. in the case of an angle). As stated above, an A or B mark is not given if a correct numerical answer arises fortuitously from incorrect working. For Mechanics questions, allow A or B marks for correct answers which arise from taking *g* equal to 9.8 or 9.81 instead of 10.

© University of Cambridge International Examinations 2012

The following abbreviations may be used in a mark scheme or used on the scripts:

AEF Any Equivalent Form (of answer is equally acceptable)

AG Answer Given on the question paper (so extra checking is needed to ensure that the detailed working leading to the result is valid)

BOD Benefit of Doubt (allowed when the validity of a solution may not be absolutely clear)

CAO Correct Answer Only (emphasising that no "follow through" from a previous error is allowed)

CWO Correct Working Only - often written by a 'fortuitous' answer

ISW Ignore Subsequent Working

MR Misread

PA Premature Approximation (resulting in basically correct work that is insufficiently accurate)

SOS See Other Solution (the candidate makes a better attempt at the same question)

SR Special Ruling (detailing the mark to be given for a specific wrong solution, or a case where some standard marking practice is to be varied in the light of a particular circumstance)

Penalties

MR -1 A penalty of MR -1 is deducted from A or B marks when the data of a question or part question are genuinely misread and the object and difficulty of the question remain unaltered. In this case all A and B marks then become "follow through √" marks. MR is not applied when the candidate misreads his own figures - this is regarded as an error in accuracy. An MR-2 penalty may be applied in particular cases if agreed at the coordination meeting.

PA -1 This is deducted from A or B marks in the case of premature approximation. The PA -1 penalty is usually discussed at the meeting.

© University of Cambridge International Examinations 2012

1 Either: Obtain value $x^3 = 27$ from inspection, equation, … B1
Obtain value $x^3 = 1$ similarly B2
Obtain $x = 1$ and $x = 3$ B1
Or: Attempt to square both sides obtaining 3 terms on LHS M1
Attempt solution for x^3 of 3-term quadratic DM1
Obtain $x^3 = 1$ and $x^3 = 27$ A1
Obtain $x = 1$ and $x = 3$ A1 [4]

2 State or imply that $\ln y = \ln A + x \ln b$ B1
Equate intercept on y-axis to $\ln A$ M1
Obtain $\ln A = 2.14$ and hence $A = 8.5$ A1
Attempt gradient of line or equivalent (or use of correct substitution) M1
Obtain $0.47 = \ln b$ or equivalent and hence $b = 1.6$ A1 [5]

3 **(i)** Substitute 2 and equate to zero or divide and equate remainder to zero M1
Obtain $a = 2$ A1 [2]

(ii) **(a)** Attempt to find quadratic factor by division, inspection or identity M1
Obtain $2x^2 + x - 3$ A1
Conclude $(x - 2)(2x + 3)(x - 1)$ A1 [3]

(b) Attempt substitution of –1 or attempt complete division by $x + 1$ M1
Obtain 6 A1 [2]

4 **(i)** Use $\sec^2 \theta = 1 + \tan^2 \theta$ B1
Attempt solution of quadratic equation in $\tan \theta$ M1
Obtain $\tan^2 \theta - 12 \tan \theta + 36 = 0$ or equivalent and hence $\tan \theta = 6$ A1 [3]

(ii) **(a)** Attempt use of $\tan(A - B)$ formula M1
Obtain $\frac{5}{7}$ following their value of $\tan \theta$ A1√ [2]

(b) Attempt use of $\tan 2\theta$ formula M1
Obtain $-\frac{12}{35}$ A1 [2]

5 **(i)** Differentiate to obtain expression of form $ke^{\frac{1}{2}x} + m$ M1
Obtain correct $2e^{\frac{1}{2}x} - 6$ A1
Equate attempt at first derivative to zero and attempt solution DM1
Obtain $\frac{1}{2}x = \ln 3$ or equivalent A1
Conclude $x = \ln 9$ or $a = 9$ A1 [5]

(ii) Integrate to obtain expression of form $ae^{\frac{1}{2}x} + bx^2 + cx$ M1
Obtain correct $8e^{\frac{1}{2}x} - 3x^2 + 3x$ A1
Substitute correct limits and attempt simplification DM1
Obtain $8e - 14$ A1 [4]

© University of Cambridge International Examinations 2012

6 **(i)** Obtain derivative of form $k(2t + 1)^{-3}$ M1
Obtain $-4(2t + 1)^{-3}$ or equivalent as derivative of x A1
Obtain $\frac{1}{2}(t + 2)^{-\frac{1}{2}}$ or equivalent as derivative of y B1
Equate attempt at $\frac{dy}{dx}$ to -1 M1
Obtain $(2p+1)^3 = 8(p+2)^{\frac{1}{2}}$ or equivalent A1
Confirm given answer $p = (p+2)^{\frac{1}{6}} - \frac{1}{2}$ A1 [6]

(ii) Use iteration process correctly at least once M1
Obtain final answer 0.678 A1
Show sufficient iterations to 5 decimal places to justify answer or show a sign change in the interval (0.6775, 0.6785) A1 [3]
[0.7 → 0.68003 → 0.67857 → 0.67847 → 0.67846]

7 **(i)** Expand to obtain $4 \sin^2 x + 4 \sin x \cos x + \cos^2 x$ B1
Use $2 \sin x \cos x = \sin 2x$ B1
Attempt to express $\sin^2 x$ or $\cos^2 x$ (or both) in terms of $\cos 2x$ M1
Obtain correct $\frac{1}{2}k(1 - \cos 2x)$ for their $k \sin^2 x$ or equivalent A1√
Confirm given answer $\frac{5}{2} + 2\sin 2x - \frac{3}{2}\cos 2x$ A1 [5]

(ii) Integrate to obtain form $px + q \cos 2x + r \sin 2x$ M1
Obtain $\frac{5}{2}x - \cos 2x - \frac{3}{4}\sin 2x$ A1
Substitute limits in integral of form $px + q \cos 2x + r \sin 2x$ and attempt simplification DM1
Obtain $\frac{5}{8}\pi + \frac{1}{4}$ or exact equivalent A1 [4]

© University of Cambridge International Examinations 2012