Cambridge Assessment International Education

# Cambridge International AS & A Level

CANDIDATE NAME

CENTRE NUMBER | | | | | |

CANDIDATE NUMBER | | | | |

*6270513510*

**MATHEMATICS** **9709/62**

Paper 6 Probability & Statistics 2 **February/March 2022**

**1 hour 15 minutes**

You must answer on the question paper.

You will need: List of formulae (MF19)

**INSTRUCTIONS**

- Answer **all** questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do **not** use an erasable pen or correction fluid.
- Do **not** write on any bar codes.
- If additional space is needed, you should use the lined page at the end of this booklet; the question number or numbers must be clearly shown.
- You should use a calculator where appropriate.
- You must show all necessary working clearly; no marks will be given for unsupported answers from a calculator.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.

**INFORMATION**

- The total mark for this paper is 50.
- The number of marks for each question or part question is shown in brackets [ ].

This document has **12** pages.


© UCLES 2022

**1** The lengths, in millimetres, of a random sample of 12 rods made by a certain machine are as follows.

200 201 198 202 200 199 199 201 197 202 200 199

**(a)** Find unbiased estimates of the population mean and variance. [3]

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

**(b)** Give a statistical reason why these estimates may not be reliable. [1]

.....

.....

.....

.....

.....

.....

.....

**2** Harry has a five-sided spinner with sectors coloured blue, green, red, yellow and black. Harry thinks the spinner may be biased. He plans to carry out a hypothesis test with the following hypotheses.

$$H_0: \text{ P(the spinner lands on blue)} = \frac{1}{5}$$
$$H_1: \text{ P(the spinner lands on blue)} \neq \frac{1}{5}$$

Harry spins the spinner 300 times. It lands on blue on 45 spins.

Use a suitable approximation to carry out Harry's test at the 5% significance level. [5]

**3** A random sample of 500 households in a certain town was chosen. Using this sample, a confidence interval for the proportion, $p$, of all households in that town that owned two or more cars was found to be $0.355 < p < 0.445$.

Find the confidence level of this confidence interval. Give your answer correct to the nearest integer. [5]

**4** In the past the time, in minutes, taken by students to complete a certain challenge had mean 25.5 and standard deviation 5.2. A new challenge is devised and it is expected that students will take, on average, less than 25.5 minutes to complete this challenge. A random sample of 40 students is chosen and their mean time for the new challenge is found to be 23.7 minutes.

**(a)** Assuming that the standard deviation of the time for the new challenge is 5.2 minutes, test at the 1% significance level whether the population mean time for the new challenge is less than 25.5 minutes. [5]

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

**(b)** State, with a reason, whether it is possible that a Type I error was made in the test in part **(a)**. [1]

.....

.....

.....

.....

.....

**5** The heights of buildings in a large city are normally distributed with mean 18.3 m and standard deviation 2.5 m.

**(a)** Find the probability that the total height of 5 randomly chosen buildings in the city is more than 95 m. [4]

**(b)** Find the probability that the difference between the heights of two randomly chosen buildings in the city is less than 1 m. [5]

**6** In a game a ball is rolled down a slope and along a track until it stops. The distance, in metres, travelled by the ball is modelled by the random variable $X$ with probability density function

$$\mathrm{f}(x) = \begin{cases} -k(x-1)(x-3) & 1 \leqslant x \leqslant 3, \\ 0 & \text{otherwise,} \end{cases}$$

where $k$ is a constant.

**(a)** Without calculation, explain why $\mathrm{E}(X) = 2$. [1]

.....

.....

.....

.....

.....

.....

**(b)** Show that $k = \frac{3}{4}$. [3]

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

**(c)** Find Var($X$). [3]

.....

.....

.....

.....

.....

.....

.....

.....

.....

One turn consists of rolling the ball 3 times and noting the largest value of $X$ obtained. If this largest value is greater than 2.5, the player scores a point.

**(d)** Find the probability that on a particular turn the player scores a point. [4]

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

**7** **(a)** Two ponds, $A$ and $B$, each contain a large number of fish. It is known that 2.4% of fish in pond $A$ are carp and 1.8% of fish in pond $B$ are carp. Random samples of 50 fish from pond $A$ and 60 fish from pond $B$ are selected.

Use appropriate Poisson approximations to find the following probabilities.

**(i)** The samples contain at least 2 carp from pond $A$ and at least 2 carp from pond $B$. [3]

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

**(ii)** The samples contain at least 4 carp altogether. [3]

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

**(b)** The random variables $X$ and $Y$ have the distributions Po($\lambda$) and Po($\mu$) respectively. It is given that

- $P(X = 0) = [P(Y = 0)]^2$,
- $P(X = 2) = k[P(Y = 1)]^2$, where $k$ is a non-zero constant.

Find the value of $k$. [4]

## Additional Page

If you use the following lined page to complete the answer(s) to any question(s), the question number(s) must be clearly shown.

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

Permission to reproduce items where third-party owned material protected by copyright is included has been sought and cleared where possible. Every reasonable effort has been made by the publisher (UCLES) to trace copyright holders, but if any items requiring clearance have unwittingly been included, the publisher will be pleased to make amends at the earliest possible opportunity.

To avoid the issue of disclosure of answer-related information to candidates, all copyright acknowledgements are reproduced online in the Cambridge Assessment International Education Copyright Acknowledgements Booklet. This is produced for each series of examinations and is freely available to download at www.cambridgeinternational.org after the live examination series.

Cambridge Assessment International Education is part of Cambridge Assessment. Cambridge Assessment is the brand name of the University of Cambridge Local Examinations Syndicate (UCLES), which is a department of the University of Cambridge.

© UCLES 2022